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Chaos-based anytime reliable coded communications over fading channels with and without information aging

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Introduction and motivation

- Control systems where observer and controller are not co-located (e.g., wireless sensor/actuator networks) are of increasing interest
 - As a consequence, the measurements received at the controller are often impaired by noise, fading, etc.
- Error-correction coding can enhance the reliability of received measurements
 - To obtain stability in the controlled system, anytime reliability (AR) must be achieved!

Introduction and motivation

- Define the error probability at time t for a symbol transmitted at time $t-d$ as $P_e(t, d)$
 - d is the delay, which is an important variable in remote control

- The codec scheme is said to be **anytime reliable** if

$$P_e(t, d) < K e^{-\beta d}, \quad \forall t, d > d_0$$

- β is the anytime exponent of the codec scheme

Introduction and motivation

- In [1], on AWGN channel, we introduced two codec schemes, based on chaos-coded modulation (CCM):
 - Adaptive-size CCM (**AS-CCM**), which has fixed spectral efficiency and adaptive instantaneous power
 - Adaptive-bandwidth CCM (**AB-CCM**), with adaptive spectral efficiency and instantaneous power
- In this paper, we analyze their performance on **fading** channels.

[1] A. Tarable and F. J. Escribano, "Chaos-Based Anytime-Reliable Coded Communications," *IEEE Systems Journal*, vol. 14, no. 2, pp. 2214-2224, June 2020

AS-CCM

- It is based on a given chaotic map f from $[0,1]$ to $[0,1]$ with invariant pdf F_f
- We define a mapper M_f , specific for map f , which is able to map a semiinfinite binary sequence $\mathbf{b} = (b_0, b_1, \dots)$ into a real value in $[0,1]$
- In the next slide, the steps of AS-CCM encoding are given

AS-CCM

- Ideally, given \mathbf{b} , we first form a sequence of chaotic samples z_1, z_2, \dots as

$$z_n = \begin{cases} \mathcal{M}_f(\mathbf{b}), & n = 1 \\ f^{(\delta_n)}(z_{n-1}), & n > 1 \end{cases}$$

- δ_n is a nonnegative integer and $f^{(\delta_n)}$ means that the chaotic map f is applied δ_n times

AS-CCM

- Then the quantized chaotic samples are obtained as

$$z_n^Q = F_f \left(\mathcal{Q}_U^{(q_n)} \left(F_f^{-1}(z_n) \right) \right)$$

- $Q^{(q_n)}_U$ is a uniform quantizer on $[0,1]$ with 2^{q_n} levels
- In practice, by a suitable choice of the mapper, the n -th quantized sample can be written as

$$z_n^Q = \mathcal{M}_f \left([\mathbf{b}_{\varepsilon_n}^n, 0, 0, \dots] \right)$$

- where $q_n = n - \varepsilon_n + 1$ and $\delta_n = \varepsilon_n - \varepsilon_{n-1}$

AB-CCM

- In AB-CCM, given a map f , we first choose a pair of initial conditions $z(0), z(1)$ in $[0,1]$
- Symbol transmitted at time n is

$$\mathbf{s}_n = (s_n^1, \dots, s_n^{q_n})$$

through $q_n = n - \varepsilon_n + 1$ orthogonal channels, where

$$s_n^i = \begin{cases} f(s_{n-1}^{i-1}), & i > 1 \\ f(z^{(b_n)}), & i = 1 \end{cases}$$

AB-CCM

- For both schemes, the receiver decodes ML and feeds back to the TX the value of ε_n , the index of the oldest information bit which is not yet reliably decoded
- Both techniques are anytime reliable on the AWGN provided that some conditions are met on the scheme and on the channel

Ax-CCM on fading channels

- Signal received when AS-CCM is used

$$r_n = \alpha_n S_n + w_n,$$

where α_n is the fading coefficient

- Signal received when AB-CCM is used

$$r_n^{(i)} = \alpha_n^{(i)} S_n^{(i)} + w_n^{(i)}, \quad i = 1, \dots, q_n.$$

- For AB-CCM, we will consider flat fading, i.e.,

$$\alpha_n^{(i)} = \alpha_n, \quad i = 1, \dots, q_n$$

Simulation results

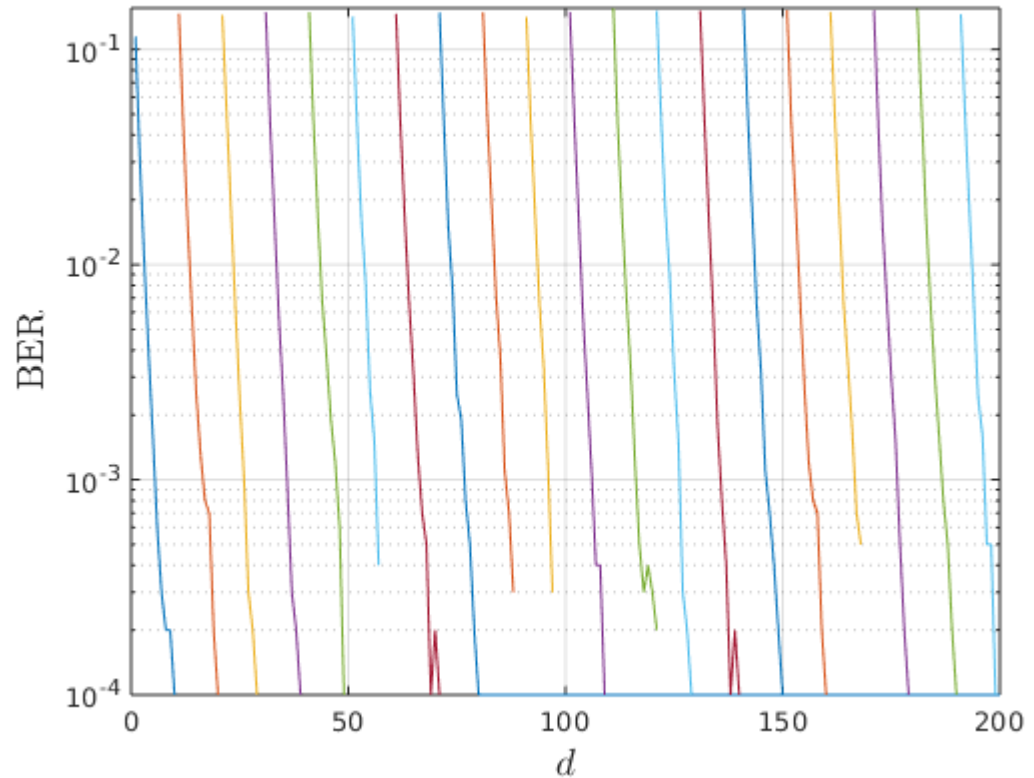
- 3 different scenarios for the flat Rician fading channel:
 - Perfect CSI at RX.
 - Perfect CSI at TX, with a threshold on the channel coefficients prior to channel gain inversion.
 - Perfect CSI at TX, with thresholding + information aging effect (channel gain information is fed back only every B blocks).
- We will present the results in terms of BER evolution as a function of the different system parameters:
 - Noise power, channel K -factor, maximum Doppler shift, threshold, updating frequency.

Simulation results

AS-CCM

- Perfect CSI at RX
- $\sigma^2 = 0.5$
- $K = 7$ dB
- $f_{max,d} = 10^{-2}$ Hz

AR is preserved

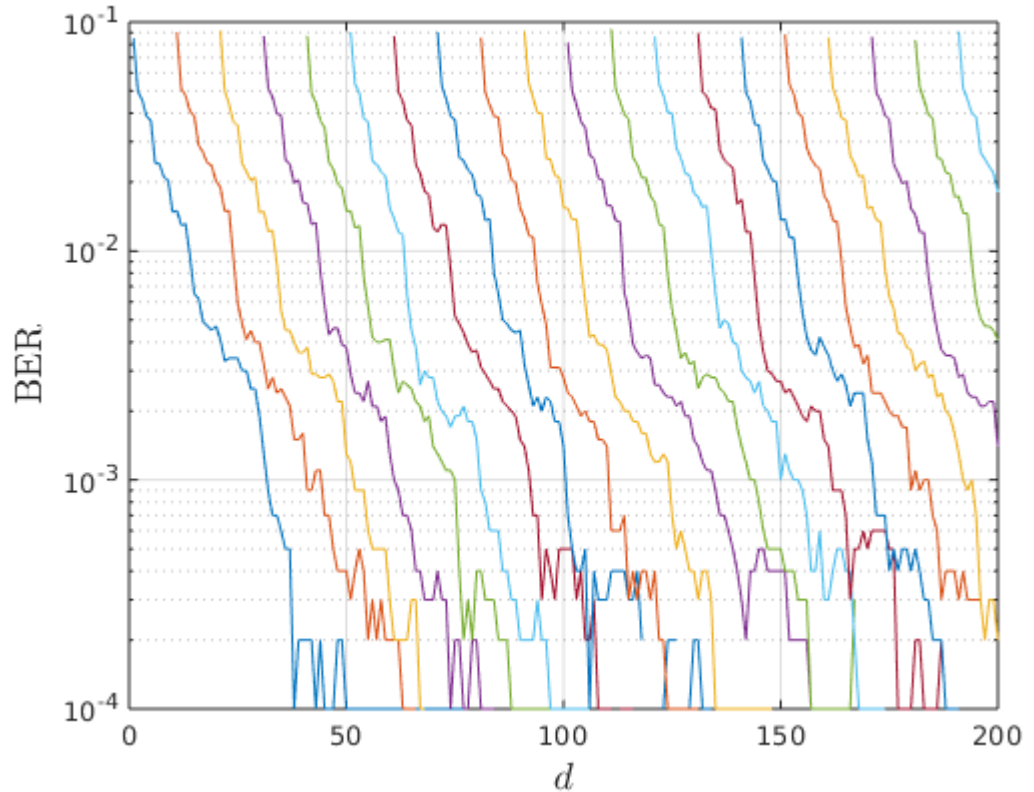


Simulation results

AB-CCM

- Perfect CSI at RX
- $\sigma^2 = 0.25$
- $K = 7$ dB
- $f_{max,d} = 10^{-2}$ Hz

AR is preserved

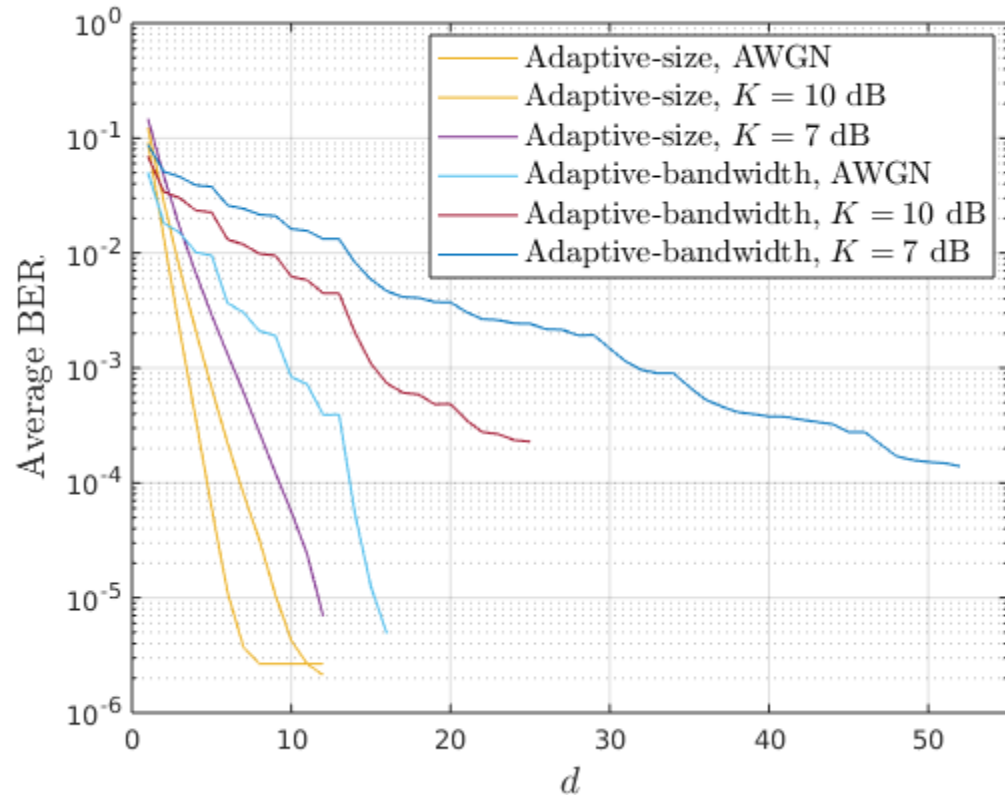


Simulation results

Average BER

- Perfect CSI at RX
- $\sigma^2 = 0.5$ (AS-CCM)
- $\sigma^2 = 0.25$ (AB-CCM)
- Different K
- $f_{max,d} = 10^{-2}$ Hz

Trends are as expected

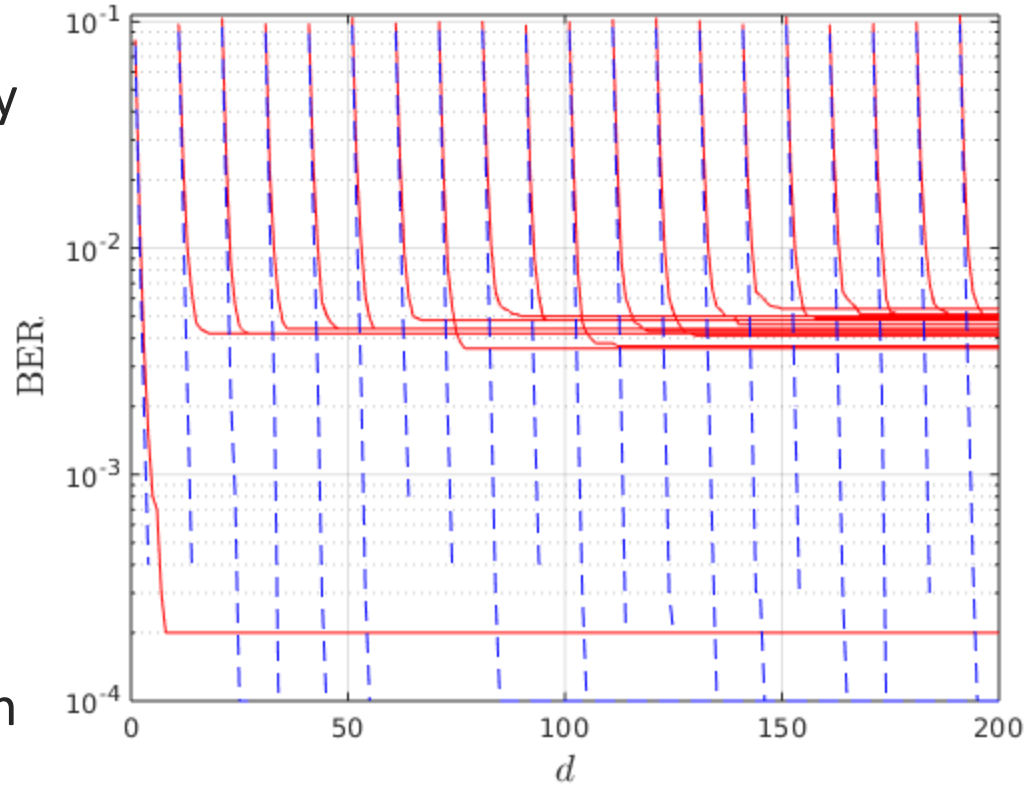


Simulation results

AS-CCM

- Perfect CSI at TX
- Channel inversion only above a threshold
- $\sigma^2 = 0.5$
- $K = 3$ dB
- $f_{max,d} = 10^{-3}$ Hz
- $\alpha_{th} = 0.1$ (red)
- $\alpha_{th} = 10^{-8}$ (blue)

AR is lost for high threshold

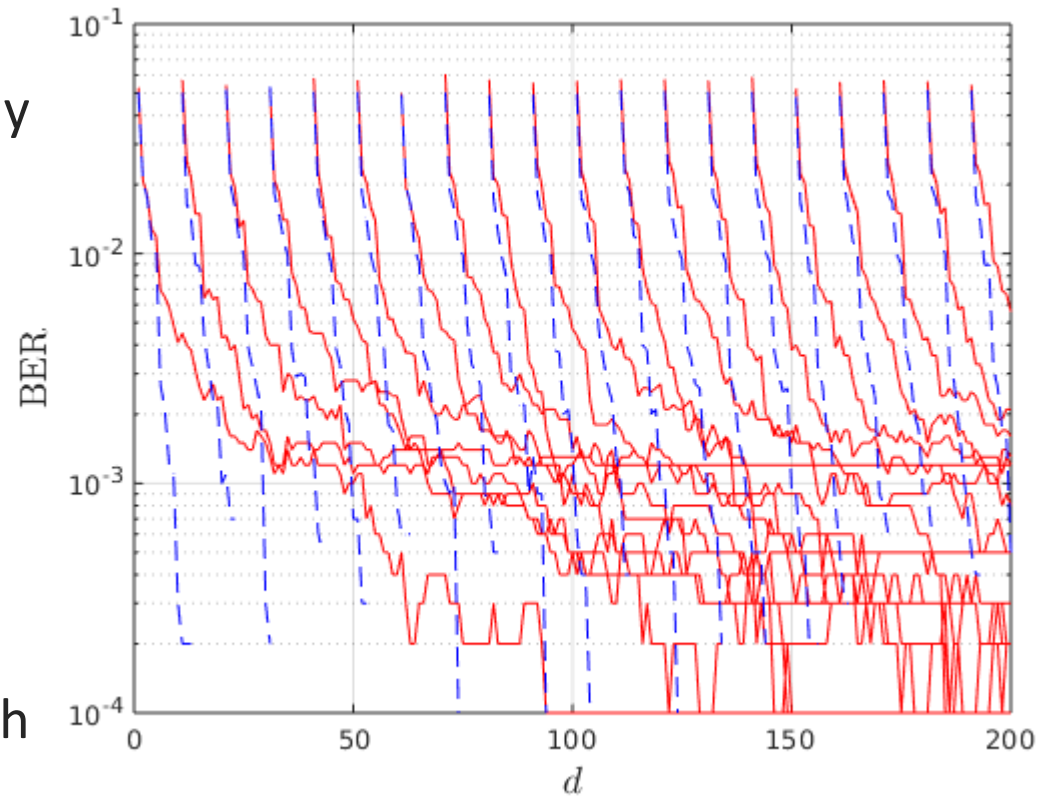


Simulation results

AB-CCM

- Perfect CSI at TX
- Channel inversion only above a threshold
- $\sigma^2 = 0.25$
- $K = 3$ dB
- $f_{max,d} = 10^{-3}$ Hz
- $\alpha_{th} = 0.1$ (red)
- $\alpha_{th} = 10^{-8}$ (blue)

AR is lost for high threshold

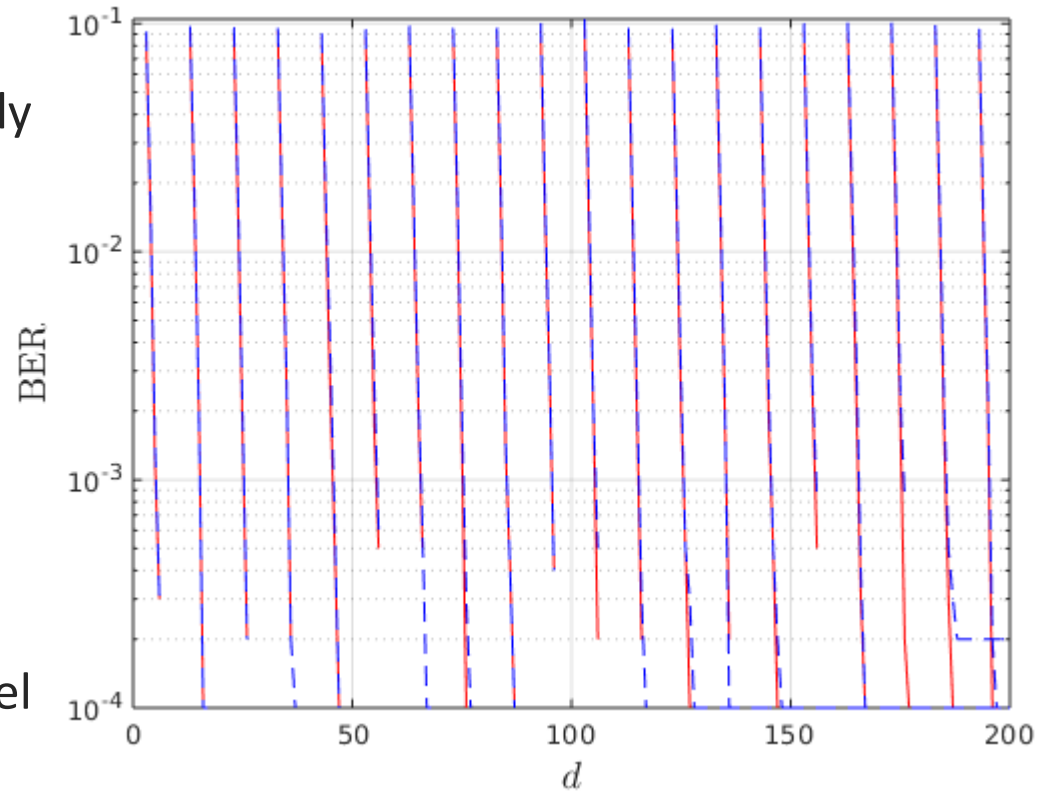


Simulation results

AS-CCM with Information Aging (IA)

- Perfect CSI at TX
- Channel inversion only above a threshold
- $\sigma^2 = 0.5$
- $K = 10$ dB
- $f_{max,d} = 10^{-2}$ Hz
- $\alpha_{th} = 0.1$
- $B = 1$ (red)
- $B = 9$ (blue)

AR is lost for low channel updating frequency

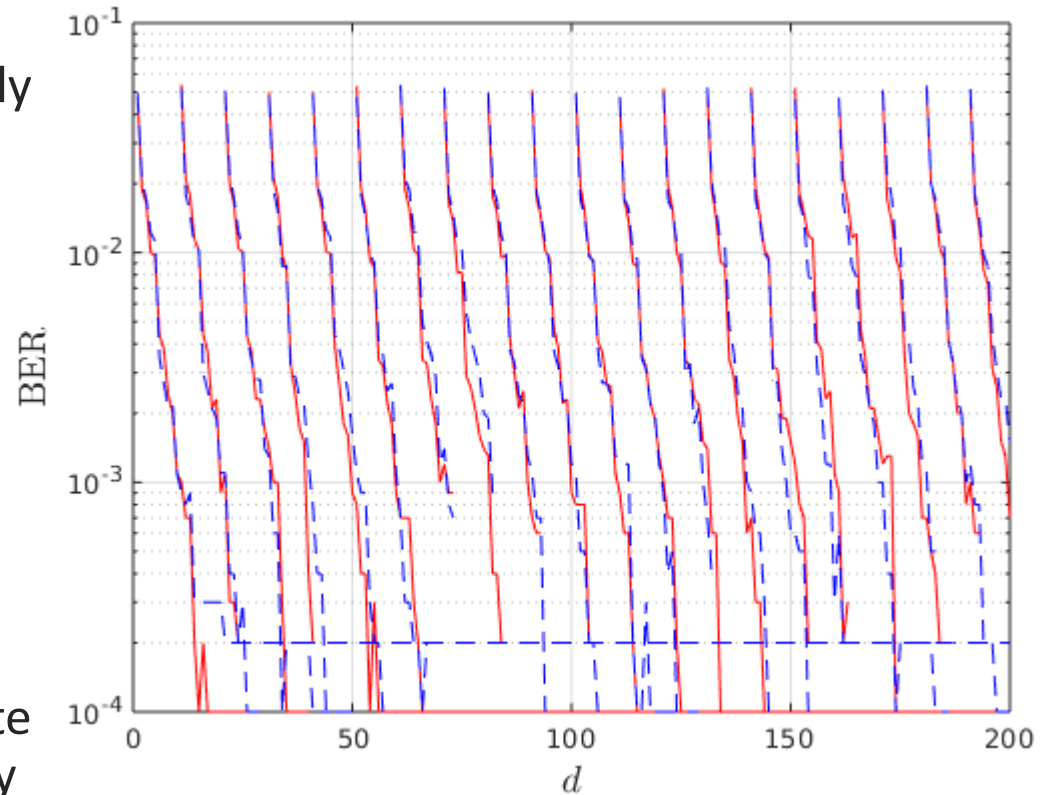


Simulation results

AB-CCM with IA

- Perfect CSI at TX
- Channel inversion only above a threshold
- $\sigma^2 = 0.25$
- $K = 7$ dB
- $f_{max,d} = 10^{-2}$ Hz
- $\alpha_{th} = 0.1$
- $B = 1$ (red)
- $B = 4$ (blue)

AR is lost for moderate channel updating frequency



Conclusions

- Two families of chaos-based AR capable systems (AS-CCM, AB-CCM) are shown to maintain AR properties in fading channels, under given conditions.
- Perfect CSI at the RX without IA leads to expected good results.
- Perfect CSI at the TX can only be reasonably applied using a threshold for channel inversion (TX power limitation).
- Thresholding affects the preservation of AR properties: high thresholds may lead to non-AR systems.
- In presence of IA (channel coefficients are fed back to the TX only every B steps), AR may not be preserved when channel update frequency is too low.

Thank you!

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