# Time Reversal in Reverberating Environments for Electromagnetic Focusing in Biological Bodies

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## Abstract

This paper proposes the time reversal as an electromagnetic focusing technique for improving deep biological tissues heating. The analysis occurred by full-wave FDTD simulations considering a body of a 6-year-old boy placed within a reverberant environment. The excitation was a pulse at the central frequency of 433.9 MHz. After the time reversal application, the distribution of the computed electromagnetic field shows excellent results in terms of strong spatial focusing within the human body. Examples are given for the head and limb.

## 1 Introduction

Biological tissue heating techniques are therapeutic medical tools that use ultrasound (US) and electromagnetic (EM) waves at high frequencies to heat biological tissues above the physiological temperature around 41-43°C. Hyperthermia, thermal ablation and diathermy are the main heating techniques used in the medical field for osteoarticular diseases and cancer treatments [1, 2]. US based techniques are mainly used for heating of the outermost biological tissues due to a low penetration range. This leaves more interest in EM heating techniques (EMHT) for deep tissue heating. EMHTs use microwaves whose frequency depends on the depth of the target tissue and on the International Telecommunication Union (ITU) Radio Regulations. Most commonly used frequencies are 434 MHz, 915 MHz and 2.45 GHz [3, 4, 5]. Despite the above-mentioned techniques are effective, the focus of EM fields in high non-homogeneity medium represents the greatest clinical challenge. Several years ago, the time reversal (TR) technique has been introduced for focusing acoustic and EM waves [7]. It consists of two main steps, in the first phase a transmitter (Tx) sends a EM signal which is recorded by a receiver (Rx), in the second phase, the recorded signal is flipped over time and re-emitted by the same Tx. At this point, the flipped and re-emitted signal focuses on the point where it was previously recorded, obtaining a similar signal to the one initially emitted [7, 8]. It has been shown that TR works even better in chaotic environments where the multiple scattering intensifies the focus of the EM wave [10, 11, 15]. Therefore, the reverberation chamber (RC) represents a great solution for TR applications. At this regard this paper proposes the TR in RC as an alternative tissue heating technique to improve EM wave focus within the human body.

## 2 Analysis description

In order to analyze the performance of the TR as tissue heating technique, numerical simulations have been performed based on the Finite-Difference Time-Domain (FDTD) method to reproduce computational electrodynamics [9]. The differential numerical modeling have been used to examine how the TR in RC affects the focusing of EM waves towards deep biological tissues.

### 2.1 Simulation set-up

The simulated domain was a RC sample by 1.0 mm cells as the tested biological tissues resolution. The walls of the RC have been made up by Perfect Electric Conductor (PEC) with zero resistance and zero tangent electric field to simulate a lossless environment with total reflection. The Tx antenna was a coaxial monopole consisting of 101 cells along the y-axis, placed in the lower left corner of the RC. The anatomical structures analyzed in the FDTD simulation were the head, the upper and the lower limbs of the Theloni body map taken from the Foundation for Research on Information Technologies in Society 1 see figure 1. The biological volume to be heated by the TR was an internal cell of each body part. The biological tissue properties used in FDTD simulations were the relative electrical permittivity $\varepsilon_r$ and the electrical conductivity $\sigma$ [14]. The model selected for the dielectric data across the frequency range was a summation of 4-Cole-Cole expressions [12] as reported below:

$$
\varepsilon_r = \varepsilon_{\infty} + \sum_{m=1}^{4} \frac{(\varepsilon_{m} - \varepsilon_{\infty})}{1 + (j\omega\tau_m)^{1-\alpha_m}} - j\frac{\sigma}{\omega\varepsilon_0} \tag{1}
$$

where $\varepsilon_r$ and $\varepsilon_{\infty}$ are the static and infinite frequency dielectric constants, $\varepsilon_0$ is the permittivity of free space, $\omega$ is the angular frequency, $\tau$ is a time constant, $\sigma$ is the conductivity and $j$ the complex variable. In the following section, the the FDTD simulation procedure is reported.

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1 https://itis.swiss/virtual-population/tissue-properties/database/
with $f_{\text{min}} = 0.3839$ GHz, $f_{\text{max}} = 0.4839$ GHz and $f_0 = 0.4339$ GHz, with medium ratio $384.6$. Given the impulse response $h(t)$ of the RC, the received signal at the cell the signal is to be focused:

$$u(t) = s(t) \otimes h(t)$$  \hspace{1cm} (5)

where $\otimes$ denotes the time convolution. Applying the well known ordinary TR procedure [13], we apply the TR mirrored signal $u(-t)$ to the Tx achieving the reconstructed response:

$$s_r(t) = u(-t) \otimes h(t)$$  \hspace{1cm} (6)

The reconstructed signal $s_r(t)$ was computed for any simulation in order to show how the re-emitted and flipped signal by the TR is mostly focused on the target cell. In the next session, the results of each simulation are reported.

### 3 Results

The simulation results were reported for the head and upper limb in terms of signal reconstruction and EM field distribution. As shown in the figure 2, the reconstructed signal in the head (top left) reproduces the emitted signal mainly in the center showing out of phase lobes at the ends. This affects the less focusing of the EM waves in the head as the EM field map for the head (top right) shows a less chaotic field distribution. According to the theory, the more chaotic the field, the better the signal reconstruction and the greater the heating at the target point. The results for the upper limb, instead, show a better signal reconstruction (lower left) without lobes at the ends and a more chaotic EM field distribution. In conclusion, the TR in RC, the RC, the received signal at the cell the signal is to be focused:

$$u(t) = s(t) \otimes h(t)$$  \hspace{1cm} (5)

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### 4 Conclusions

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### 5 Acknowledgements

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### References

Figure 2. On the left $s_r(t) \text{ vs } s(t)$ are reported for the head and the upper limbs. On the right the EM field at the peak of the $s_r(t)$ are reported for the head, upper limbs.


[14] C. Gabriel. Compilation of the Dielectric Properties of Body Tissues at RF and Microwave Frequencies, Re-